

Experimental study of direct photon emission in $K^- \rightarrow \pi^- \pi^0 \gamma$ decay using ISTRAP+ detector

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Abstract

The branching ratio in the charged-pion kinetic energy region of 55 to 90 MeV for the direct photon emission in the $K^- \rightarrow \pi^- \pi^0 \gamma$ decay has been measured using in-flight decays detected with the ISTRAP+ setup operating in the 25 GeV/c negative secondary beam of the U-70 PS. The value

$$Br(DE) = [0.37 \pm 0.39 (\text{stat}) \pm 0.10 (\text{syst})] \times 10^{-5}$$

obtained from the analysis of 930 completely reconstructed events is consistent with the average value of two stopped-kaon experiments, but it differs by 2.5 standard deviations from the average value of three in-flight-kaon experiments. The result is also compared with recent theoretical predictions.

1 Introduction

The radiative decay channel $K^- \rightarrow \pi^- \pi^0 \gamma$ ($K_{\pi 2\gamma}$) is one of the most sensitive and important channels in investigating the chiral anomaly [1] in the non-leptonic sector [2, 3]. This chiral anomaly is a basic feature of quantum field theories with chiral fermions and thus of the Standard Model. Therefore, experimental tests of the chiral anomaly are crucial for the theoretical basis of particle physics.

The total amplitude for the $K_{\pi 2\gamma}$ decay can be generally decomposed as the sum of two terms: the inner bremsstrahlung (IB) associated with the decay $K^- \rightarrow \pi^- \pi^0$ ($K_{\pi 2}$) in which the photon is emitted from the outgoing charged pion, and the direct emission (DE) in which the photon is emitted from one of the intermediate states of the decay. The inner bremsstrahlung is completely predicted by quantum electrodynamics in terms of the $K_{\pi 2}$ amplitude [4]. Because the $K_{\pi 2}$ decay is suppressed by the $\Delta I = 1/2$ isospin selection rule, the bremsstrahlung contribution to the $K_{\pi 2\gamma}$ decay is also suppressed. Unlike the bremsstrahlung, the direct emission processes are permitted here, since for them weak-electromagnetic transitions are possible from the initial kaon to the final two-pion P -wave state with $I = 1$. Although the inner bremsstrahlung component is still dominant, it can be isolated kinematically, and therefore the direct emission contribution can compete with the suppressed inner bremsstrahlung one.

The simplest radiative transitions for the direct emission in the $K_{\pi 2\gamma}$ decay are electric $E1$ and magnetic $M1$ dipole transitions [5]. The electric transition can interfere with the inner bremsstrahlung process, and possible non-standard-model effects, like a CP -violating asymmetry between $K_{\pi 2\gamma}^+$ and $K_{\pi 2\gamma}^-$ decay rates, could appear in the corresponding interference term. The magnetic transition is a manifestation of the chiral anomaly.

Within the framework of Chiral Perturbation Theory (ChPT) at leading order, $O(p^4)$, the magnetic transition amplitude consists of two different classes of anomalous amplitudes: reducible [2] and direct [3, 6] amplitudes. The reducible anomalous amplitude is derived directly from the Wess–Zumino–Witten functional [7] and does not depend on undetermined constants, whereas the direct anomalous amplitude, arising from higher-dimension operators in ChPT, and also the electric transition amplitude are subject to some theoretical uncertainties.

The differential rate for the $K_{\pi 2\gamma}$ decay is conveniently expressed in terms of the Dalitz plot variables T_c^* and W , where T_c^* is the kinetic energy of π^- in the K^- rest frame, and $W^2 \equiv (p \cdot q)(p_c \cdot q) / (m_{\pi^-}^2 m_{K^-}^2)$. Here p , p_c and q are 4-momenta of K^- , π^- and γ , and m_{π^-} and m_{K^-} are masses of π^- and K^- , respectively. This rate can be written [8] in terms of the inner bremsstrahlung differential rate as

$$\frac{\partial^2 \Gamma}{\partial T_c^* \partial W} = \frac{\partial^2 \Gamma_{IB}}{\partial T_c^* \partial W} \left\{ 1 + 2 \frac{m_{\pi^-}^2}{m_{K^-}^2} \operatorname{Re} \left[\frac{E}{eA} \right] W^2 + \frac{m_{\pi^-}^4}{m_{K^-}^2} \left(\left| \frac{E}{eA} \right|^2 + \left| \frac{M}{eA} \right|^2 \right) W^4 \right\}, \quad (1)$$

where A is the on-shell amplitude for the $K_{\pi 2}$ decay, and E and M are the direct emission electric and magnetic invariant dimensionless amplitudes, defined in Ref. [2].

In experimental studies of the $K_{\pi 2\gamma}$ decay the variable T_c^* is usually used to minimize contaminations arising from the $K_{\pi 2}$ decay, dominated at $T_c^* > 90$ MeV, and from the decay $K^- \rightarrow \pi^- \pi^0 \pi^0$ ($K_{\pi 3}$), dominated at $T_c^* < 55$ MeV. The variable W is convenient to isolate the inner bremsstrahlung from the direct emission, since the former process dominates at small values of W , while the latter dominates at large values of W .

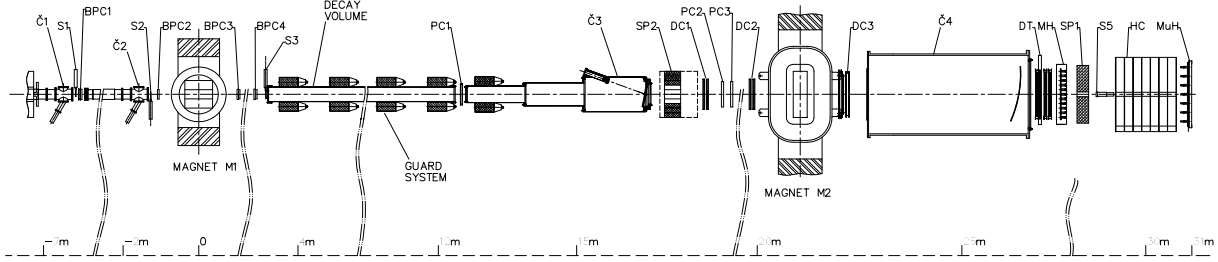


Figure 1: The side elevation view of the ISTR A+ detector.

The branching ratio in the region of $55 \text{ MeV} < T_c^* < 90 \text{ MeV}$ for the direct photon emission in the $K_{\pi 2\gamma}^\pm$ decay (Br) has been measured in the following five experiments: three in-flight-kaon and two stopped-kaon experiments have found the weighted average values of $Br = (1.8 \pm 0.4) \times 10^{-5}$ [9, 10, 11] and $Br = (0.44 \pm 0.08) \times 10^{-5}$ [12, 13], respectively. The discrepancy between these two average values is 3.3 standard deviations. Therefore, further experimental studies are necessary to settle this discrepancy.

The cited experimental values of Br can be compared with corresponding theoretical predictions in the same T_c^* region. Under the assumption that the direct emission is entirely due to the reducible anomalous amplitude given by Eq. (30b) in Ref. [2] with standard $O(p^2)$ ChPT coupling constants, ChPT at leading order predicts the value of $Br = 0.35 \times 10^{-5}$. Model-dependent theoretical predictions which take into account the additional contribution of the direct anomalous amplitude [3, 6] are also available: for example, the factorization model [6] predicts the value of $Br = 1.94 \times 10^{-5}$.

The above-mentioned observations encourage us to perform a new measurement of the direct photon emission in the $K_{\pi 2\gamma}$ decay using in-flight negative kaons.

2 Experimental setup

The experiment has been performed at the IHEP proton synchrotron U-70 with the experimental apparatus ISTR A+, which is a modification of the ISTR A-M setup [14] and which was described in some details in our recent papers where studies of the K_{e3}^- [15], $K_{\mu 3}^-$ [16] and $K_{\pi 3}^-$ [17] decays were presented. The setup is located in the negative un-separated secondary beam with the following parameters during the measurement: the momentum is $\sim 25 \text{ GeV}/c$ with $\sigma(p)/p \sim 1.5\%$, the admixture of kaons is $\sim 3\%$, and the total intensity is $\sim 3 \times 10^6$ per spill.

The side elevation view of the ISTR A+ detector is shown in Fig. 1. The setup coordinate system is the following: the x , y and z axes are turned along the field of the spectrometer magnet M2, the vertical line and the setup longitudinal axis, respectively.

The measurement of the beam particles, deflected by the beam magnet M1, is performed with four beam proportional chambers BPC1–BPC4. The kaon identification is done by three threshold gas Cherenkov counters Č0–Č2 (Č0 is not shown in Fig. 1). The momenta of the secondary charged particles, deflected in the vertical plane by the spectrometer magnet M2, are measured with three proportional chambers PC1–PC3, three drift chambers DC1–DC3 and four planes of the drift tubes DT. The secondary photons are detected by the lead-glass electromagnetic calorimeters SP1 and SP2. To veto low energy photons the decay volume is surrounded by the guard system of eight lead-glass

rings and by the SP2. The wide aperture threshold helium Cherenkov counters Č3 and Č4 are not used in the present study. In Fig. 1, HC is a scintillator-iron sampling hadron calorimeter, MH is a scintillation hodoscope used to improve the time resolution of the tracking system, MuH is a scintillation muon hodoscope.

The trigger is provided by the scintillation counters S1–S5, the Cherenkov counters Č0–Č2 and the analog sum of the amplitudes from the last dinodes of the calorimeter SP1 (see Refs. [15, 16] for details). The latter serves to suppress the dominating $K^- \rightarrow \mu^- \bar{\nu}_\mu$ decay.

3 Event selection

About 332 M events were collected during one physics run in Winter 2001. These experimental data are complemented by about 260 M events generated with the Monte Carlo program GEANT3 [18]. The Monte Carlo simulation includes a realistic description of the experimental setup: the decay volume entrance windows, the track chamber windows, gas mixtures, sense wires and cathode structures, the Cherenkov counter mirrors and gas mixtures, the showers development in the electromagnetic calorimeters, etc. The details of the reconstruction procedure have been published in Refs. [15, 16], here only key points relevant to the $K^- \rightarrow \pi^- \pi^0 \gamma$ event selection are described.

The data processing starts with the beam track reconstruction in the beam proportional chambers BPC1–BPC4, and then with the secondary tracks reconstruction in the decay tracking system PC1–PC3, DC1–DC3 and DT. The decay vertex is reconstructed by means of the unconstrained vertex fit of the beam and decay tracks. Finally, the electromagnetic showers are looked for in the calorimeters SP1 and SP2, and the photons are reconstructed using the fit procedure with the Monte Carlo generated two-dimensional patterns of showers. To suppress leptonic K^- decays the particle identification is used. The electrons are identified using the ratio of the energy of the shower, detected in the calorimeter SP1 and associated with the track of the electron, to the momentum of the electron [15]. The muons are identified using the information from the calorimeters SP1 and HC [16].

In the present study, the main purpose of the event selection is to suppress significantly all components of the background contamination, even if some of them are negligible in studying the K^- decay modes which branching ratios are more than 1%. The expediency of the selection criteria, mentioned below, is motivated by the Monte Carlo investigation.

At the first step of the event selection only the measurements of the beam and secondary charged particles are used. Those events are selected which satisfy the following requirements:

- only one beam track and one negative secondary track are detected;
- the first hit of the secondary track is either in the chamber PC1, or in the DC1, or in the PC2, while the last hit of this track is in the drift tubes DT;
- the probability of the vertex fit, $CL(\chi^2)$, is more than 10^{-4} ;
- the relative error of the secondary track momentum, $\sigma(p)/p$, is less than 0.1;
- the decay vertex is before the calorimeter SP2 ($6 \text{ m} < z < 17 \text{ m}$), and its transverse position is in the region of ($-3 \text{ cm} < x < 3 \text{ cm}$, $-2 \text{ cm} < y < 6 \text{ cm}$);

- the secondary track is not identified as an electron or as a muon;
- the angle between the K^- line of flight and the π^- direction in the K^- rest frame is in the region of $-0.8 < \cos \theta_{\pi^-}^* < 0.85$;
- the π^- kinetic energy in the K^- rest frame is in the region of 55 to 90 MeV.

At the second step of the event selection the measurements of the showers in the calorimeters SP1 and SP2 are used. Associating the SP1 shower with the secondary track is done if the distance $R = [(x_{sh} - x_{tr})^2 + (y_{sh} - y_{tr})^2]^{1/2}$ is less than 3 cm, where (x_{sh}, y_{sh}) and (x_{tr}, y_{tr}) are the transverse coordinates of the shower and of the track extrapolation to the calorimeter SP1, respectively. The event selection is done by the requirements:

- the number of showers associated with the secondary track (N_{ass}) is no more than one, and if the event has such shower (i.e. $N_{ass} = 1$) the ratio of the energy of this shower to the track momentum is less than 0.7;
- the total (in both calorimeters) number of photons (i.e. showers, which are not associated with the secondary track) is equal to three.

Also, the events are selected if the three photons satisfy the following requirements:

- at least one of them is detected in the SP1;
- the photon energy is more than 0.8 GeV, but is more than 1 GeV if the photon is detected in the SP2;
- the relative error of the photon energy, $\sigma(E)/E$, is less than 1, but the number of photons with $\sigma(E)/E > 0.2$ is no more than one;
- the relative transverse position of the SP1 photon ($\Delta x = x_{sh} - x_{tr}$, $\Delta y = y_{sh} - y_{tr}$) is outside the rectangle region of ($|\Delta x| < 7$ cm, $|\Delta y| < 11$ cm) and, if $N_{ass} = 1$, the strip region of ($|\Delta x| < 2$ cm, $\Delta y \geq 11$ cm);
- the photon configuration is not such as the one, in which all SP1 photons are reconstructed from one and the same cluster of overlapped showers.

At the third step of the event selection the hits found in the hodoscope MH, in the proportional chamber PC1 and in the drift tubes DT are considered to minimize the background contamination and systematics. The further selection is done by the requirements:

- the number of hits in the hodoscope MH (n_{MH}) is no less than one, and exactly one of them is associated with the secondary track extrapolation to the hodoscope, all the others (if $n_{MH} > 1$) are associated with the SP1 photon interpolations to the hodoscope (in terms of the distance in the MH transverse plane, $r < 10$ cm);
- the number of hits, which are found in the chamber PC1, but not used in the track reconstruction, is no more than one for each coordinate plane;
- if some hit found in the y -coordinate plane of the chamber PC1 is used in the secondary track reconstruction, the decay vertex is in the region before this chamber;

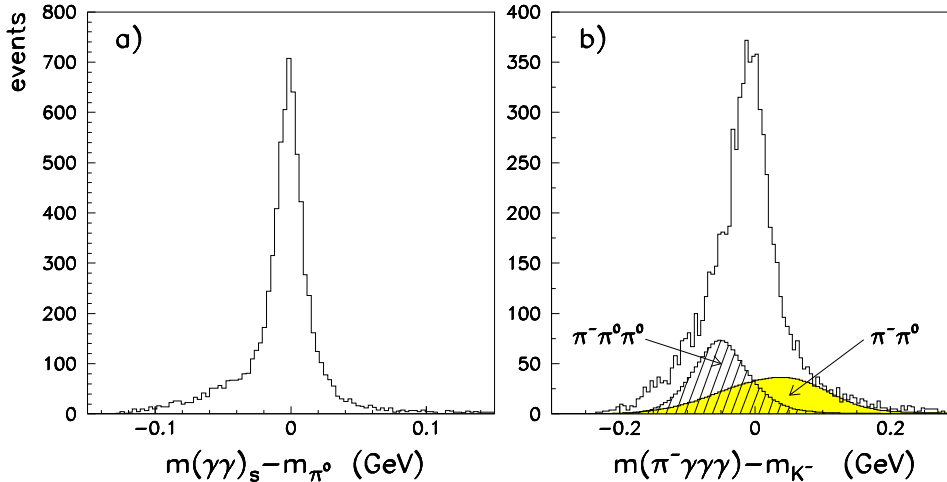


Figure 2: Mass deviations in the events after the third step of the event selection: **a)** the deviation from the π^0 mass, $m(\gamma\gamma)_s - m_{\pi^0}$, of the effective mass of the $\gamma\gamma$ pair with the smallest absolute value of the deviation; **b)** the deviation from the K^- mass, $m(\pi^-\gamma\gamma) - m_{K^-}$, of the effective mass of the $\pi^-\gamma\gamma$ system, together with the Monte Carlo estimated background contaminations of the $K^- \rightarrow \pi^-\pi^0\pi^0$ and $K^- \rightarrow \pi^-\pi^0$ events (hatched histograms).

- any hit found in the DT x - or y -coordinate plane is either used in the track reconstruction or associated with at least one SP1 photon interpolation to the drift tubes (in terms of the distance in the DT coordinate plane, $\delta x < 1$ cm or $\delta y < 1$ cm).

To illustrate the quality of the first three steps of the event selection the mass deviations $m(\gamma\gamma)_s - m_{\pi^0}$ and $m(\pi^-\gamma\gamma) - m_{K^-}$ for the corresponding events are shown in Fig. 2, where $m(\gamma\gamma)_s$ is the effective mass of the $\gamma\gamma$ pair with the smallest absolute value of the deviation, $m(\pi^-\gamma\gamma)$ is the effective mass of the $\pi^-\gamma\gamma$ system, and m_{π^0} is the π^0 mass. The background contamination of the $K^- \rightarrow \pi^-\pi^0\pi^0$ and $K^- \rightarrow \pi^-\pi^0$ events (also shown in Fig. 2b) is estimated from the Monte Carlo simulation to be 41%.

At the fourth step of the event selection the kinematic criteria are used to select the $K^- \rightarrow \pi^-\pi^0\gamma$ events. First, for each of the three $\gamma\gamma$ combinations in the event, assuming it arises from the $\pi^0 \rightarrow \gamma\gamma$ decay, the kinematic 5C-fit for the $K^- \rightarrow \pi^-\pi^0\gamma$ hypothesis is applied. Then, such $\pi^0 \rightarrow \gamma\gamma$ pairing is chosen, for which the event passes the kinematic fit with the largest value of the combined probability $P_c = P_{fit} P_{IB}$, where P_{fit} is the χ^2 probability of the fit and P_{IB} is the inner bremsstrahlung decay probability as a function of the *fitted* values of the Dalitz plot variables.

After that, the event selection is done restricting the allowed ranges of the variables defined by the *measured* values of the particle momenta. The corresponding criteria, in which the measured π^0 four-momentum is multiplied (re-scaled) by a factor $\lambda = m_{\pi^0}/m(\gamma\gamma)$, are the following:

- the measured momentum of the $\pi^-\pi^0\gamma$ system is in the region of 23 to 29 GeV/ c ;
- the angle between the measured $\pi^-\pi^0$ and γ transverse momenta defined with respect to the K^- direction is more than 154° (see Fig. 3a);
- the ratios, $p_{fit}(\pi^0)/p_{meas}(\pi^0)$ and $p_{fit}(\gamma)/p_{meas}(\gamma)$, of the fitted π^0 and γ momenta values to the measured ones are in the region of 0.8 to 1.2 (see Fig. 3b);

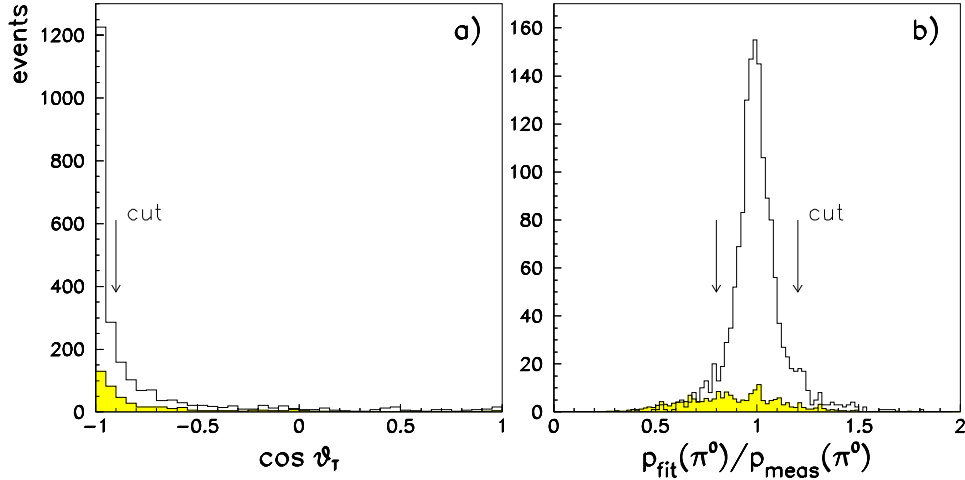


Figure 3: Distributions of the events passed the kinematic 5C-fit for the $K^- \rightarrow \pi^- \pi^0 \gamma$ hypothesis, together with the Monte Carlo estimated background contaminations of the $K^- \rightarrow \pi^- \pi^0 \pi^0$ and $K^- \rightarrow \pi^- \pi^0$ events (hatched histograms): **a)** the angle, θ_T , between the measured $\pi^- \pi^0$ and γ transverse momenta defined with respect to the K^- direction; **b)** the ratio, $p_{fit}(\pi^0)/p_{meas}(\pi^0)$, of the fitted π^0 momentum value to the measured one.

- the deviations $|m(\gamma\gamma) - m_{\pi^0}|$ and $|m(\pi^- \pi^0 \gamma) - m_{K^-}|$ are less than $40 \text{ MeV}/c^2$;

where $m(\gamma\gamma)$ is the effective mass of the $\gamma\gamma$ pair arising from the π^0 decay, $m(\pi^- \pi^0 \gamma)$ is the effective mass of the $\pi^- \pi^0 \gamma$ system.

At the fifth step of the event selection the contaminations of the $K^- \rightarrow \pi^- \pi^0 \pi^0$ and $K^- \rightarrow \pi^- \pi^0$ events are minimized. The event is not selected if, for at least one $\pi^0 \rightarrow \gamma\gamma$ pairing, it passes the kinematic fit for the $K^- \rightarrow \pi^- \pi^0 \pi^0$ (one γ in the event is lost) or $K^- \rightarrow \pi^- \pi^0$ (one γ in the event is a calorimeter noise) hypothesis and satisfies the additional requirements, which for the $K^- \rightarrow \pi^- \pi^0 \pi^0$ hypothesis are:

- the Dalitz plot variable W (defined for the chosen above $K^- \rightarrow \pi^- \pi^0 \gamma$ hypothesis) is more than 0.25;
- the deviation $|m(\pi^- \pi^0 \pi^0) - m_{K^-}|$ is less than $40 \text{ MeV}/c^2$, where $m(\pi^- \pi^0 \pi^0)$ is the effective mass of the $\pi^- \pi^0 \pi^0$ system, in which the first π^0 is reconstructed from the measured photons and re-scaled as above by a factor λ , while the second one is calculated from the balance of the three-momenta;
- the deviation $|M_X(\pi^- \pi^0) - m_{\pi^0}|$ is less than $40 \text{ MeV}/c^2$, where $M_X(\pi^- \pi^0)$ is the missing mass to the $\pi^- \pi^0$ system with the reconstructed and re-scaled π^0 meson (see Fig. 4a);

and which for the $K^- \rightarrow \pi^- \pi^0$ hypothesis are:

- the angle between the measured π^- and π^0 transverse momenta defined with respect to the K^- direction is more than 174° ;
- the deviation $|m(\pi^- \pi^0) - m_{K^-}|$ is less than $50 \text{ MeV}/c^2$, where $m(\pi^- \pi^0)$ is the effective mass of the $\pi^- \pi^0$ system with the re-scaled π^0 meson;

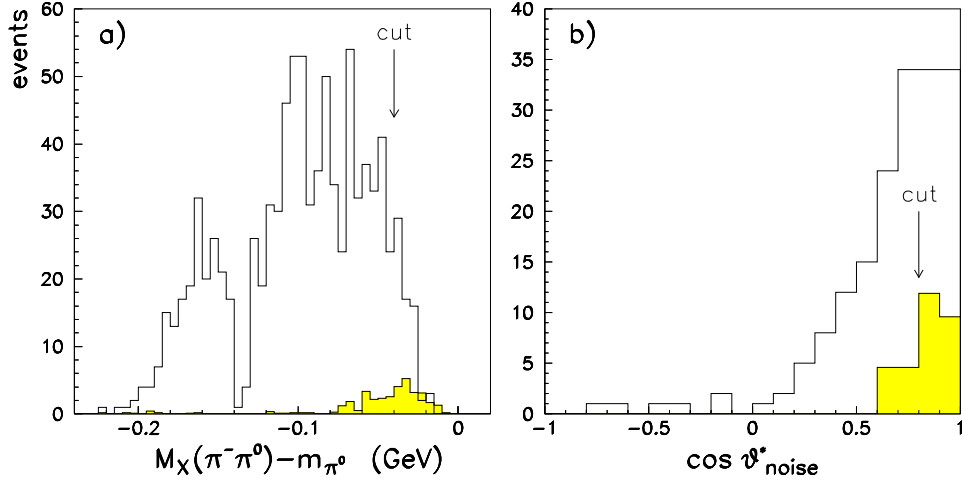


Figure 4: Distributions of the events before the last cut of the fifth step of the event selection, together with the Monte Carlo estimated background contaminations (hatched histograms): **a)** for the $K^- \rightarrow \pi^- \pi^0 \pi^0$ hypothesis, the deviation from the π^0 mass, $M_X(\pi^- \pi^0) - m_{\pi^0}$, of the missing mass to the $\pi^- \pi^0$ system with the reconstructed and re-scaled π^0 meson; **b)** for the $K^- \rightarrow \pi^- \pi^0$ hypothesis, the angle in the K^- rest frame, θ_{noise}^* , between the π^- and γ (considered as a calorimeter noise) momenta.

- the angle in the K^- rest frame between the π^- and γ (the latter is considered here as a calorimeter noise) momenta is less than 37° (see Fig. 4b).

Using the mentioned above selection criteria for the $K^- \rightarrow \pi^- \pi^0 \gamma$ decay we have collected 930 completely reconstructed events. The corresponding numbers of accepted Monte Carlo events are about 13 times larger than the ones collected in the experiment. The surviving background contamination arising from all background decay modes is estimated from the Monte Carlo simulation to be less than 6%. The detailed event reduction statistics is given in Table 1.

Table 1: The event reduction statistics.

Total number of events	332 M
Beam track reconstructed	248 M
Secondary track(s) reconstructed	124 M
Number of events written on DST	108 M
K^- and π^- selected (all cuts of the 1st step)	1729 K
$\gamma\gamma\gamma$ selected (all cuts of the 2nd and the 3rd steps)	7623
$K^- \rightarrow \pi^- \pi^0 \gamma$ pre-selected (all cuts of the 4th step)	1041
$K^- \rightarrow \pi^- \pi^0 \gamma$ selected (all cuts of the 5th step)	930

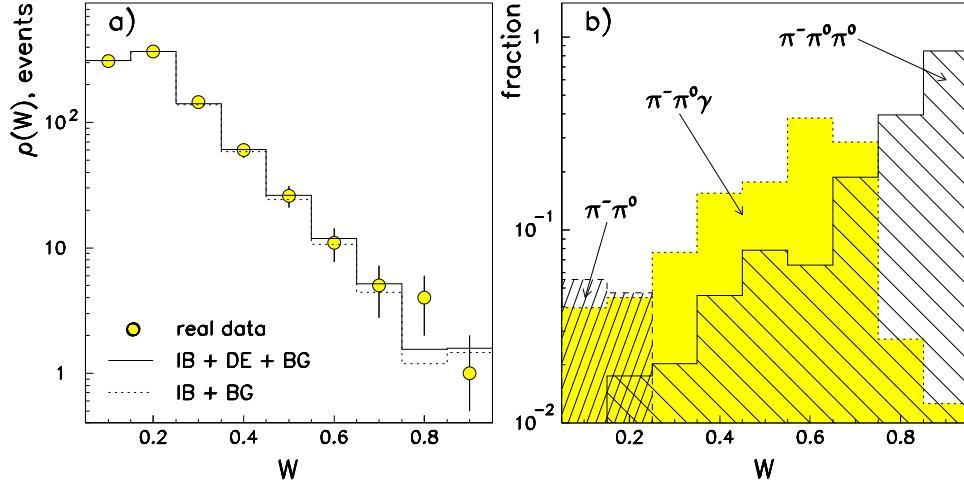


Figure 5: Dependences on the Dalitz plot variable W : **a)** the uncorrected number of the selected $K^- \rightarrow \pi^- \pi^0 \gamma$ events, together with the corresponding Monte Carlo estimations (the full line is the sum of the IB, DE and BG components, but the dotted line is the sum of the IB and BG ones); **b)** the Monte Carlo estimated fractions in the selected $K^- \rightarrow \pi^- \pi^0 \gamma$ events of the contaminations arising from the background $K^- \rightarrow \pi^- \pi^0$ and $K^- \rightarrow \pi^- \pi^0 \pi^0$ decays and from the wrong reconstructed $K^- \rightarrow \pi^- \pi^0 \gamma$ decay.

4 Analysis

In the present analysis, the uncorrected distribution $\rho(W)$ of the selected $K^- \rightarrow \pi^- \pi^0 \gamma$ events as a function of the Dalitz plot variable W was used. This distribution is shown in Fig. 5a together with the normalized distribution of the Monte Carlo simulated events reconstructed with the same program as for the real data. The background was estimated from the simulation of the particle interaction with the material of the detector and of the kaon decay including all decay modes with the branching ratios more than 1%. The corresponding branching ratios and matrix elements in the Monte Carlo simulation were taken from the PDG [19].

The Monte Carlo distribution in Fig. 5a includes the $K^- \rightarrow \pi^- \pi^0 \gamma$ component (with and without the direct emission) and the background contamination (BG). The fractions in the selected $K^- \rightarrow \pi^- \pi^0 \gamma$ events of the contaminations arising from the background $K^- \rightarrow \pi^- \pi^0$ and $K^- \rightarrow \pi^- \pi^0 \pi^0$ decays are shown in Fig. 5b as a function of the variable W and estimated to be 4% and 2%, respectively. The background of all other decay modes is negligible. Due to the detector imperfection, the $K^- \rightarrow \pi^- \pi^0 \gamma$ component in the simulated events consists of the correct and wrong reconstructed $K^- \rightarrow \pi^- \pi^0 \gamma$ decays. The fraction of the latter is also shown in Fig. 5b and estimated to be 6%.

Fig. 6a shows two W -dependences of the ratio of the DE and IB components estimated from the Monte Carlo $K^- \rightarrow \pi^- \pi^0 \gamma$ events without the contamination of the background decay modes. The first dependence was obtained from the *generated* events taken “before passing the detector”, while the second one was obtained from the *simulated* events taken “after passing the detector”. Comparing these dependences, one can conclude that in the present experiment the DE component is not smeared due to the detector imperfection: the acceptance and inefficiency, the event selection, the experimental resolution, the noise, the secondary interactions and the wrong $\pi^0 \rightarrow \gamma \gamma$ pairing.

The passing rate for the $K^- \rightarrow \pi^- \pi^0 \gamma$ events, $P = N_{sim}/N_{gen}$, is shown in Fig. 6b as a

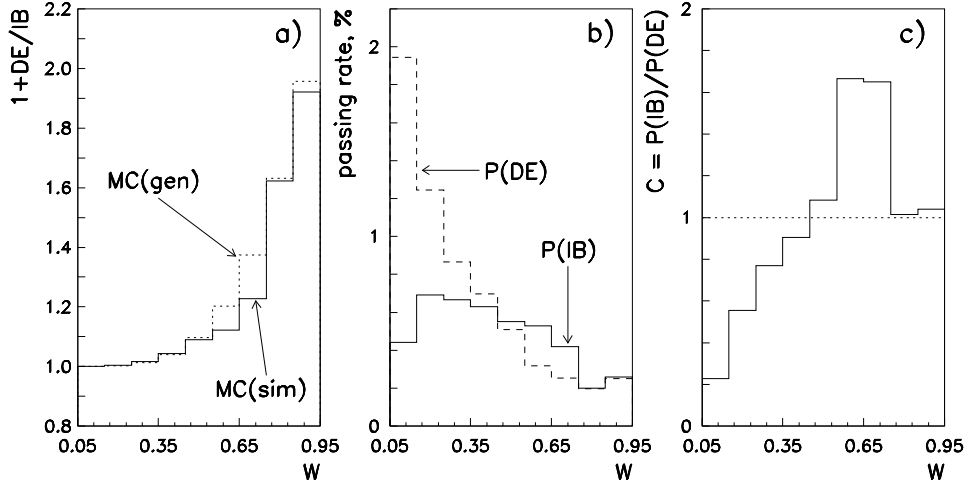


Figure 6: Dependences on the variable W estimated from the Monte Carlo $K^- \rightarrow \pi^- \pi^0 \gamma$ events without the contamination of the background decay modes: **a)** the ratio $1+DE/IB$ for the generated (dotted line) and for the simulated (full line) events; **b)** the event passing rates for the IB (full line) and for the DE (dashed line) components; **c)** the ratio of the passing rates for the IB and DE components.

function of the variable W separately for the IB and DE components. These dependences were obtained from the Monte Carlo $K^- \rightarrow \pi^- \pi^0 \gamma$ events without the contamination of the background decay modes: N_{gen} (N_{sim}) is the number of the generated (simulated) events, and the binning is given by the generated (simulated) value of the variable W . Fig. 6c shows the ratio of the passing rates for the IB and DE components,

$$C = \frac{P(IB)}{P(DE)}. \quad (2)$$

To determine the DE amplitude M in Eq. (1) (under the assumption that the DE amplitude E in Eq. (1) is equal to zero) the experimental distribution $\rho(W)$ was fitted by the method of least squares with the function

$$\rho(W)_{fit} = \alpha [\rho(W)_{BG} + \rho(W)_{IB} + \beta \rho(W)_{DE}], \quad (3)$$

where $\rho(W)_{BG}$ is the background contamination obtained from the Monte Carlo simulated $K^- \rightarrow \pi^- \pi^0$ and $K^- \rightarrow \pi^- \pi^0 \pi^0$ events only, $\rho(W)_{IB}$ and $\rho(W)_{DE}$ are the IB and DE components obtained from the Monte Carlo simulated $K^- \rightarrow \pi^- \pi^0 \gamma$ events without the contamination of the background decay modes, α and β are free parameters in the fit. This method allows to avoid the systematic errors [20] due to the “migration” of the events on the Dalitz plot because of the finite experimental resolution.

5 Results

The result of the least squares fit of Eq. (3) to the distribution $\rho(W)$ is illustrated in Fig. 7, where the corrected experimental ratio

$$R(W)_{exp} = 1 + C \cdot \left[\frac{\rho(W) - \alpha \rho(W)_{BG}}{\alpha \rho(W)_{IB}} - 1 \right] \quad (4)$$

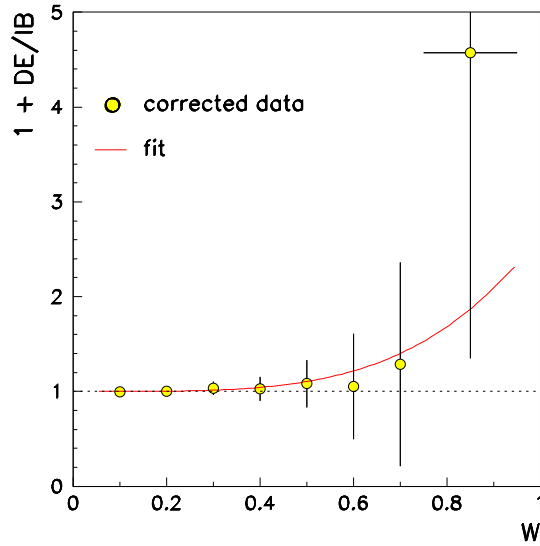


Figure 7: The corrected experimental ratio of the DE and IB components for the $K^- \rightarrow \pi^- \pi^0 \gamma$ decay as a function of W in the region of $55 \text{ MeV} < T_c^* < 90 \text{ MeV}$. The curve is the prediction of Eq. (1) with the fitted value of the amplitude M and with $E = 0$.

of the DE and IB components for the $K^- \rightarrow \pi^- \pi^0 \gamma$ decay is shown as a function of W in the T_c^* region of 55 to 90 MeV. In Eq. (4), the correction factor C given by Eq. (2) takes into account the detector imperfection, the $\alpha \rho(W)_{\text{BG}}$ term takes into account the contamination of the background decay modes, and the fitted value of α provides the normalization. The curve in Fig. 7 is predicted by Eq. (1) with the fitted value of the amplitude M (given by the fitted value of β) and with $E = 0$.

From the least squares fit with the value of $\chi^2/ndf = 2.1/7$, the direct emission component was obtained to be

$$|M| = (1.9 \pm 1.0 \pm 0.3) \times 10^{-7},$$

$$Br(DE)/Br(IB) = (1.4 \pm 1.5 \pm 0.4) \%$$

under the assumption that there is no interference component. Then, comparing this with the theoretical value of the inner bremsstrahlung branching ratio, $Br(IB) = 2.61 \times 10^{-4}$ [8], the direct emission branching ratio was determined to be

$$Br(DE) = (0.37 \pm 0.39 \pm 0.10) \times 10^{-5}$$

for the $K^- \rightarrow \pi^- \pi^0 \gamma$ decay in the region of $55 \text{ MeV} < T_c^* < 90 \text{ MeV}$. Here the first errors are statistical and the second ones are systematic.

In the determination of the systematic uncertainty of $Br(DE)$ the following sources of systematics were investigated.

- The branching ratios and matrix elements of the background decay modes used in the Monte Carlo simulation were varied within their errors ($\Delta Br = 0.01$).
- The variations of the signal and background components in the Monte Carlo simulation were allowed ($\Delta Br = 0.06$).

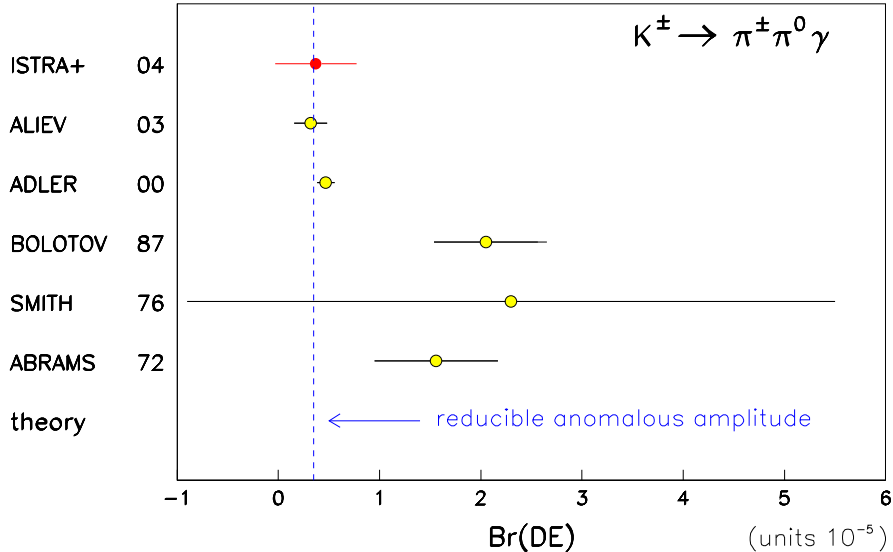


Figure 8: The branching ratio for the direct photon emission in the $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decays in the region of $55 \text{ MeV} < T_c^* < 90 \text{ MeV}$ in comparison with the theoretical prediction under the assumption that the direct emission is entirely due to the reducible anomalous amplitude [2].

- The upper edge of the decay vertex position was varied along the setup axis between the chamber PC1 and the calorimeter SP2 ($\Delta Br = 0.03$).
- The electromagnetic showers in the calorimeter SP2 were not used in the photon reconstruction ($\Delta Br = 0.01$).
- The particle identification of the secondary track was not used ($\Delta Br = 0.02$).
- The energy threshold of the selected photons was varied from the value of 0.8 GeV to 2 GeV ($\Delta Br = 0.02$).
- The variations of the angular and mass deviation cuts were applied ($\Delta Br = 0.03$).
- The event selection was done with different restrictions applied to the relative transverse positions of the SP1 photons with respect to the secondary track extrapolation ($\Delta Br = 0.04$).
- The allowed intervals for the ratios $p_{fit}(\pi^0)/p_{meas}(\pi^0)$ and $p_{fit}(\gamma)/p_{meas}(\gamma)$ were varied ($\Delta Br = 0.05$).

6 Summary and conclusion

The branching ratio for the direct photon emission in the $K^- \rightarrow \pi^- \pi^0 \gamma$ decay in the region of $55 \text{ MeV} < T_c^* < 90 \text{ MeV}$ has been measured using the ISTRA+ spectrometer. The results of our measurement and the previous experiments [9–13] on the $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decays are presented in Fig. 8. Our value of the branching ratio $Br(DE)$ is consistent with the average value of $(0.44 \pm 0.08) \times 10^{-5}$, obtained from the results of the stopped-kaon experiments [12, 13], but it differs by 2.5 standard deviations from the average value of $(1.8 \pm 0.4) \times 10^{-5}$, obtained from the results of the in-flight-kaon experiments [9–11].

The theoretical prediction for $Br(DE)$, under the assumption that the direct photon emission is entirely due to the reducible anomalous amplitude [2], is also shown in Fig. 8 for the same T_c^* region. Our result supports the hypothesis that the dominant contribution to the direct photon emission is due to the pure magnetic transition given by the reducible anomalous amplitude and the other magnetic and electric amplitudes are small or cancelled.

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